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Free fall - falling under gravity.

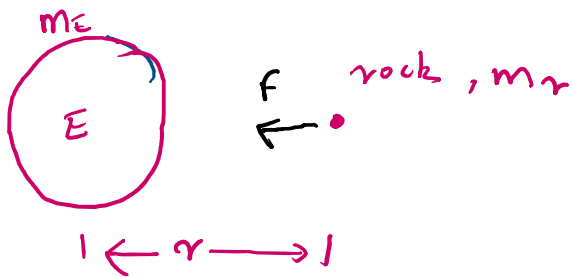
Universal Law of gravitation

$F = G \frac{m_1 m_2}{r^2}$

$G \equiv$ gravitational constant.

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- This force is only appreciable when one of the masses or both is/are astronomical >

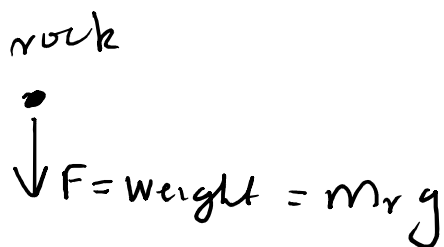


$$F = G \frac{M_E M_r}{r^2}$$

$$= \text{weight}$$

$$= m_r g$$

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$$F = m a$$

$$\therefore \cancel{m_r} a = \cancel{m_r} g$$

$$a = g$$

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rock

↓ $F = \text{weight} = m_r g$

Earth

$$F = ma$$

$$\therefore \cancel{m_r} a = \cancel{m_r} g$$

$$a = g$$

Any falling object falls with acceleration $a = g$
 $g = 9.8 \text{ m/s}^2$

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At any location on Earth, and in the absence of air resistance all objects fall with same constant acceleration:

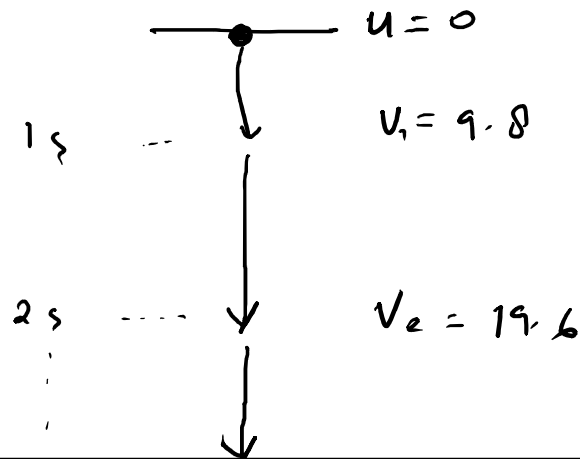
This acc. is called acceleration due to gravity, g .

approx. $g \approx 9.8 \text{ m/s}^2$

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$$a = g = 9.8 \text{ m/s}^2.$$

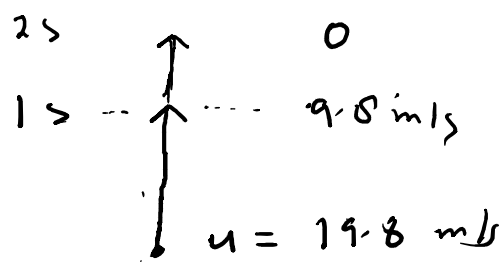
An object falling has its speed increasing at a rate of 9.8 m/s per second.



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$$a = g = 9.8 \text{ m/s}^2.$$

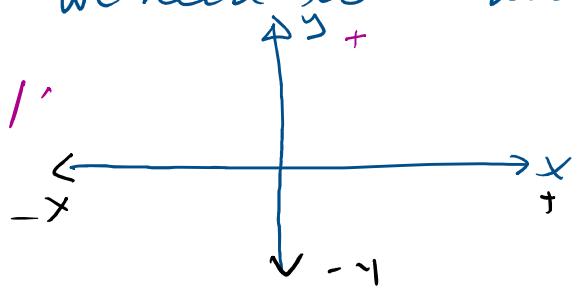
An object going up has its speed decrease at a rate of 9.8 m/s per second.



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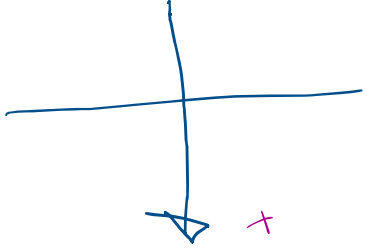
- Since acceleration is known, $a = g$
we need to choose a convention.

1.



↑ + ↓ - up positive
or
↓ - down positive

2.



Once you stick to it, choose your convention.

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Let's choose ↑ + ↓ -

↓ $a = -g$

acc. due to gravity always points down!

So: $a = -9.8 \text{ m/s}^2$

Car 10

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$\uparrow + \downarrow -$
 $\downarrow \bar{a}$
 Earth

$a = -g \rightarrow$ acc. due gravity is always pointing down.

10 m/s^2 or 9.8 m/s^2

$v = u + at$ $v^2 = u^2 + 2as$ $s = ut + \frac{1}{2}at^2$	$\rightarrow v = u - gt$ $\rightarrow v^2 = u^2 - 2gs$ $\rightarrow s = ut - \frac{1}{2}gt^2$ $s = \bar{v}t$
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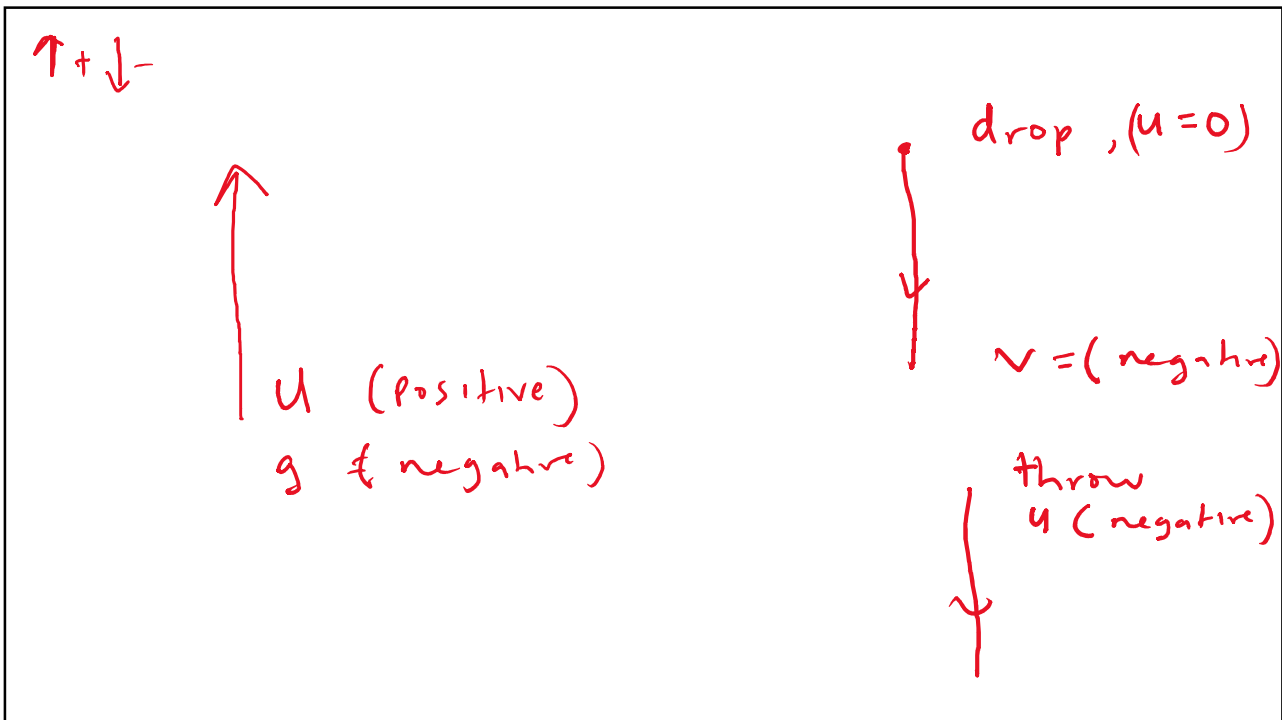
$g = 9.8 \text{ m/s}^2$

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Launch point -

— This is where an object is launched.

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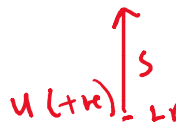
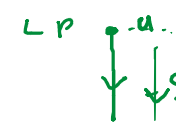
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The sign of the velocity or displacement tells you a great deal of information about the motion

	Velocity	displacement (s)
↑ + ↓ - u (+ve) = LP s	+ve object is going up	The object travels s distance above the launch point

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The sign of the velocity or displacement tells you a great deal of information about the motion

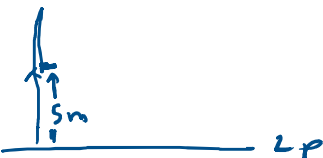
$\uparrow + \downarrow -$		Velocity	displacement (s)
	+ve	object is going up	The object travels s distance above the launch point
	-ve	object is going down	The object travels s distance below the launch point.

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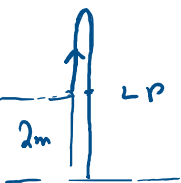
Consider an object below



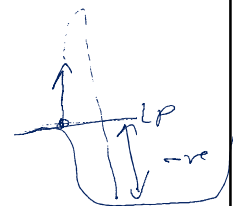
$$s = 0 = \text{displacement}$$



$$s = 5\text{m} = \text{displacement}$$



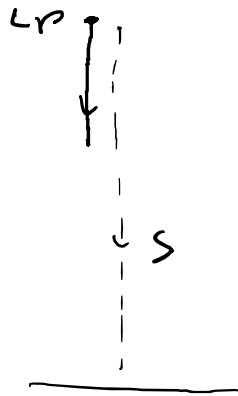
$$s = -2\text{m} = \text{displacement}$$



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EXAMPLE 2-10 Falling from a tower. Suppose that a ball is dropped ($v_0 = 0$) from a tower. How far will it have fallen after a time $t_1 = 1.00$ s, $t_2 = 2.00$ s, and $t_3 = 3.00$ s? Ignore air resistance.

drop : $u = 0$, $a = -g$.

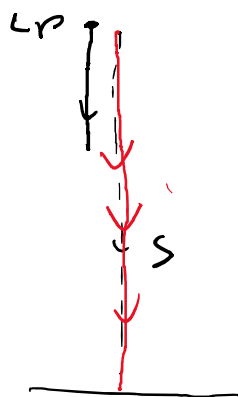


$$\begin{aligned}
 s_1 &= ut + \frac{1}{2}at^2 \\
 &= ut - \frac{1}{2}gt^2 \\
 &= ut - 4.9t^2 \\
 &= 0 - 4.9(1) \\
 &= \underline{-4.9\text{m}}
 \end{aligned}$$

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EXAMPLE 2-10 Falling from a tower. Suppose that a ball is dropped ($v_0 = 0$) from a tower. How far will it have fallen after a time $t_1 = 1.00$ s, $t_2 = 2.00$ s, and $t_3 = 3.00$ s? Ignore air resistance.

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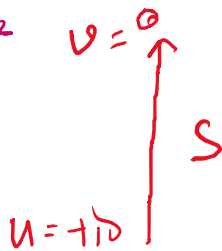
$$\begin{aligned}
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 \end{aligned}$$

dropped 4.9m below the launch point

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An object is thrown with a speed of 10 m/s. a) what is its speed after 0.5 s
 b) what is its speed after 2 sec
 c) How high does it go?

↑+ $a = -g = -9.8 \text{ m/s}^2$
 ↓- $u = +10 \text{ m/s}$



$$v^2 = u^2 + 2as$$

$$0 = 10^2 + 2(-9.8)s$$

$$s = \frac{100}{2(9.8)} = \underline{\underline{\quad}}$$

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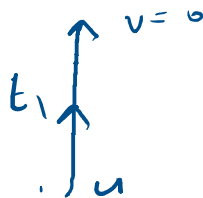
A ball is thrown upward with a velocity of 10 m/s. How long is it in the air.

time of flight

$$u = +10 \text{ m/s}, a = -g$$

$$v = 0$$

1. find t_1 to peak



$$v = u + at$$

$$0 = 10 + (-9.8)t_1$$

$$t_1 = 10/9.8 =$$

$$t_1 = 1.02 \text{ s}$$

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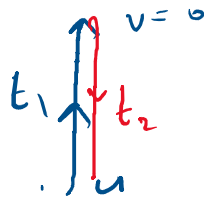
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$$v = u + at$$

$$0 = 10 + (-9.8)t_1$$

$$t_1 = 10/9.8 =$$

$$t_1 = 1.02 \text{ s}$$

Takes same time to return:

$$\therefore t = 2 \times 1.02 = 2.04 \text{ s}$$

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A ball is thrown upward with a velocity of 10 m/s. How long is it in the air -

time of flight

$$u = +10 \text{ m/s}, a = -g$$

$$v = 0$$

2. Direct: $s = ut - 4.9t^2$

$$\uparrow s = 0; \quad 0 = 10t - 4.9t^2$$

$$t = \frac{10}{4.9} = 2.04 \text{ s}$$

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