

Newton's laws of Motion

Forces

Mechanics — Kinematics
— Dynamics

Kinematics → does not care what
cause the motion

Dynamics → Study motion,
interrogate what
caused the motion

Causes of Motion

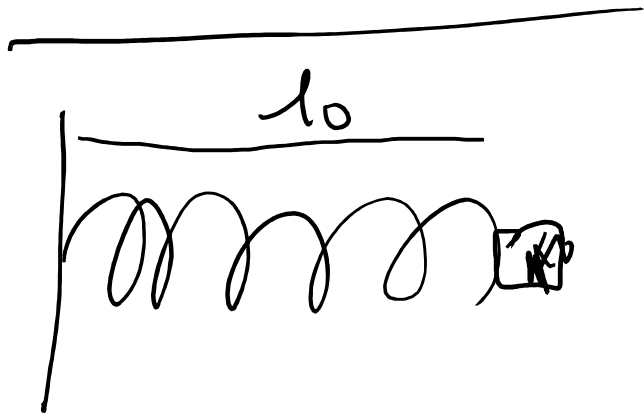
— Force

✓ **

Elastic potential energy

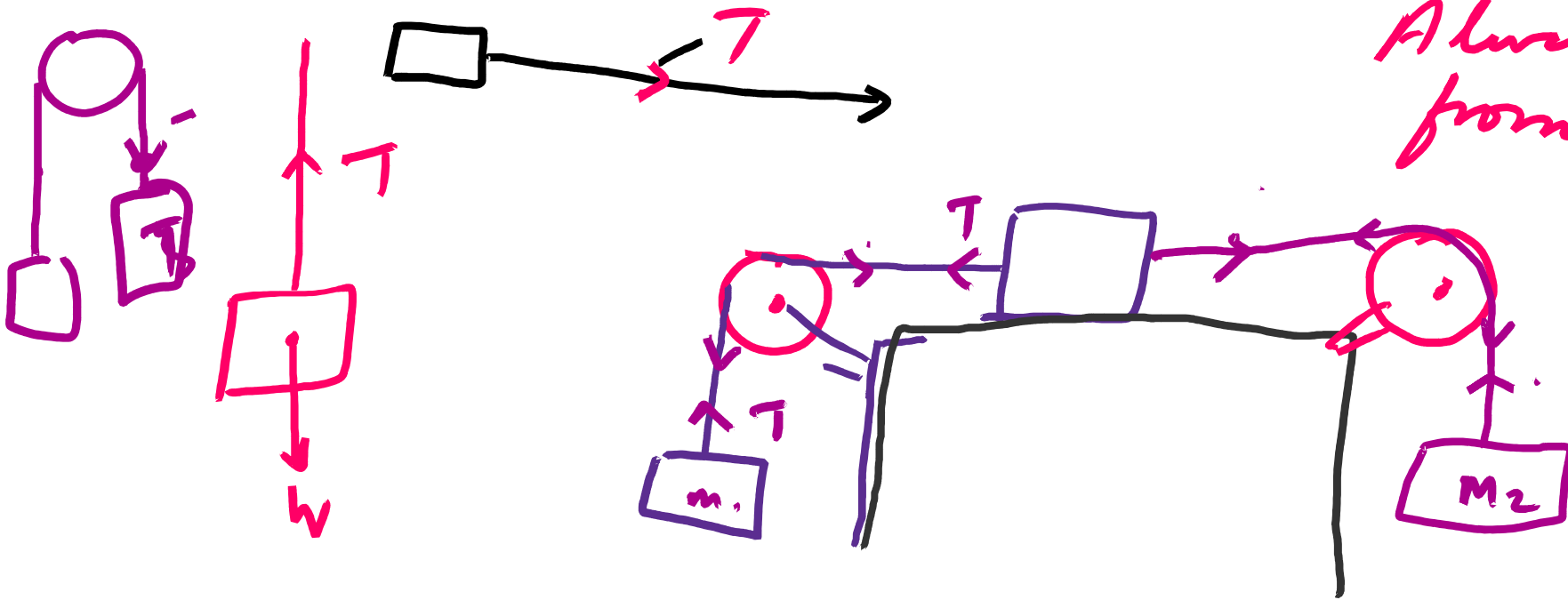
— Energy

✓ **



Types of forces

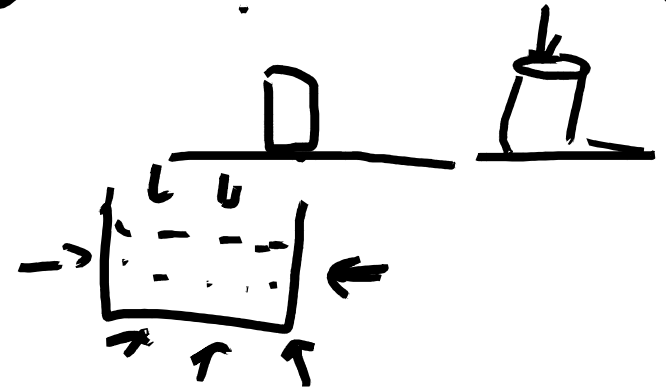
1. Tension - forces that pull on objects via strings, cables, ropes or other materials attached to objects



Always away from a body.

2. Force of Compression

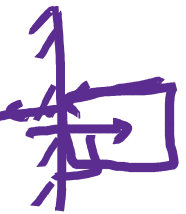
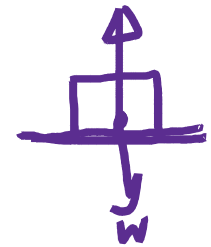
- Forces involving rigid objects which support a heavy weight (shelves, floors, benches etc)



- fluid pressure

colliding objects

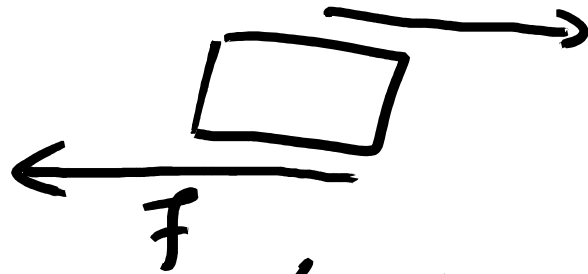
- Forces that occur perpendicular to the areas of contact, when solid objects are pushed together



3. Forces of friction

Forces that resist motion

- Sliding, slipping
- parallel to the direction of the motion

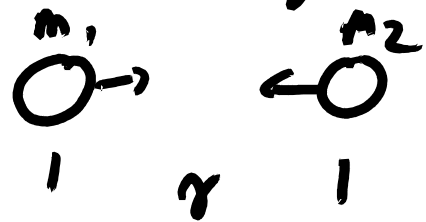


- Parallel but opposite to the direction of motion

4. Fundamental forces

- act on objects separated
in space

a) Attractive force of gravity



$$F_g = G \frac{m_1 m_2}{r^2} = \text{Weight} \\ = mg$$

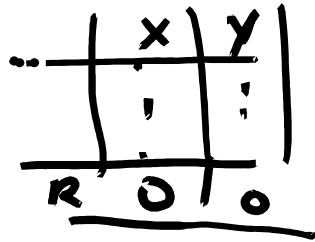


b) Electric force b/w objects possessing
electrical charge. $\ominus \quad \oplus \quad E = k q_1 q_2 / r^2$

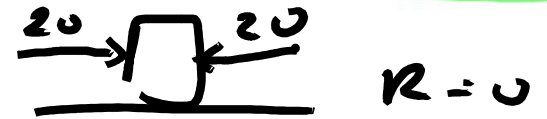
b) Magnetic force \rightarrow

Newton's Laws of Motion

- They are 3 laws.



1. a) An object at rest remains at rest if there is no resultant force acting on it



b) A moving object continues to move with constant velocity if the vector sum of ~~other~~ forces acting on it are zero
 $R=0: \Sigma F=0$: Treating vectors

Newton's Laws of Motion

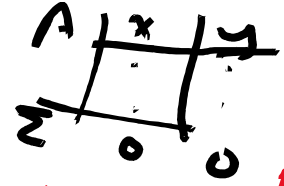
1. N- First Law of Motion

"Every object continues in its state of rest or uniform motion in a straight line unless ^{a net} ~~any~~ external force acts on it"

- An object has constant velocity (which may be zero) until a force acts on it
- The first law defines what cause motion & acceleration.

In mathematical terms

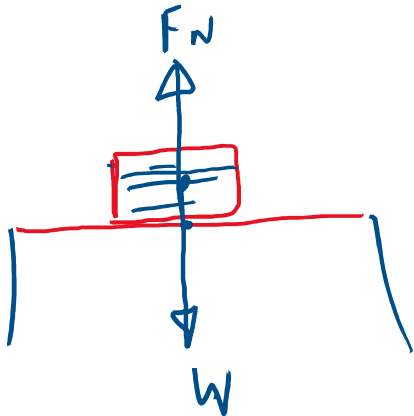
If a body has a # of forces F_1, F_2, F_3, \dots acting on it, it will remain in constant motion / rest only if



$\Sigma \equiv$ Sigma
Summation

$$\Sigma F = 0 \quad \checkmark$$

$F_N \equiv$ normal force

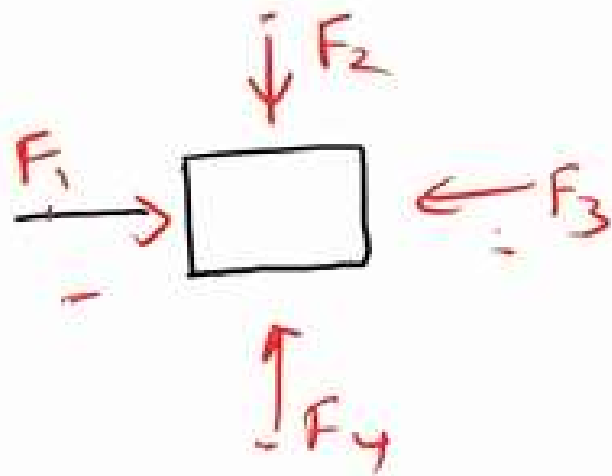


$$F_N + (-W) = 0$$
$$F_N = W : \text{balance}$$



$$\Sigma F = 0$$
$$20 + (-20) = 0$$

If multiple forces act on an object, the 1st law still applies when an object is at rest or moving with constant velocity



1.

ve	x	y
F_1	F_1	0
F_2	0	$-F_2$
F_3	$-F_3$	0
F_4	0	F_4
R	0	0

$$\sum F_x = 0$$

$$F_1 + (-F_3) = 0$$

$$F_1 = F_3$$

$$\sum F_y = 0$$

$$F_4 + (-F_2) = 0$$

$$F_4 = F_2$$

$$F_1 + 0 - F_3 = 0$$

$$F_1 = F_3$$

$$0 - F_2 + 0 + F_4 = 0$$

$$F_2 = F_4$$

1st Law - Summary.

An object at rest will remain at rest or if moving will continue moving at constant velocity unless there is a resultant force that acts on it [or as long as the resultant force is zero]

$$\sum F = 0 : \quad \begin{array}{l} v = 0 \\ v = \text{constant} \end{array}$$

Inertia

- Closely linked to the first law is the concept of Inertia.
- Inertia is the tendency of an object at rest to remain at rest & of an object in motion to remain in motion with its original velocity.
- Inertia \equiv mass

Whiplash



- Neck bones are rather delicate and can be fractured by even a moderate force.
- Fortunately the neck muscles are relatively strong and are capable of absorbing a considerable amount of energy.
- If, however, the impact is sudden, as in a rear-end collision, the body is accelerated in the forward direction by the back of the seat, and the unsupported neck is then suddenly yanked back at full speed.
- Here the muscles do not respond fast enough and all the energy is absorbed by the neck bones, causing the well-known whiplash injury).

Consequences of 1st Law.

The neck & head tries to continue at its original speed but the body accelerates →

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The neck & head tries to continue at its original speed but the body accelerates →

Newton's Second Law.

- The net force (resultant force) acting on an object is proportional to the acceleration

$$F_{\text{net}} \propto a ; F_{\text{net}} = k a$$

$$F_{\text{net}} = m a$$

But the net force
is

Newton's Second Law.

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$$F_{\text{net}} \propto a \quad ; \quad F_{\text{net}} = k a$$

$$F_{\text{net}} = m a$$

But the net force
is Resultant

$$\therefore \Sigma F = m a$$

$\Sigma F = ma$: Add the force vectorially

$$\Sigma F_x = ma_x$$

Add the forces in the x -direction
and equate to ma_x .

$$\Sigma F_y = ma_y$$

Add the forces in the y -dir
and equate to ma_y

$$\Sigma F_z = ma_z$$

$$\Sigma F = ma$$

Add the force vectorially

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Add the forces in the y-dir and equate to ma_y

$$\Sigma F_z = ma_z$$

All this means

$$\Sigma F = m a$$

force	X-Comp	Y-Comp
F_1	F_{1x}	F_{1y}
F_2	F_{2x}	F_{2y}
F_3	F_{3x}	F_{3y}
ΣF		

$$\Sigma F = ma$$

force	X-Comp	Y-Comp
F_1	F_{1x}	F_{1y}
F_2	F_{2x}	F_{2y}
F_3	F_{3x}	F_{3y}
ΣF	ΣF_x	ΣF_y

||
 ma_x

||
 F_{net}

||
 ma_y

||
 F_{net}

A net force of one Newton is that force that causes an acceleration of 1 m/s^2 on a 1 kg mass.

$$1 \text{ N} = (\text{kg}) \text{ m/s}^2 = 1 \text{ kg m/s}^2 = \text{N}$$

What does **net** mean?

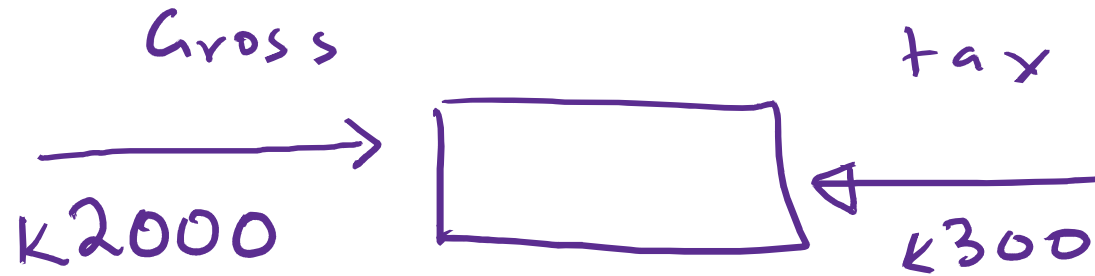
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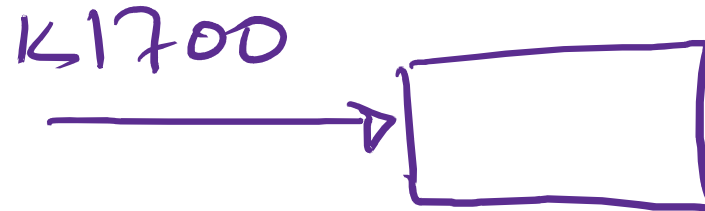
What does **net** mean?

Unbalanced!

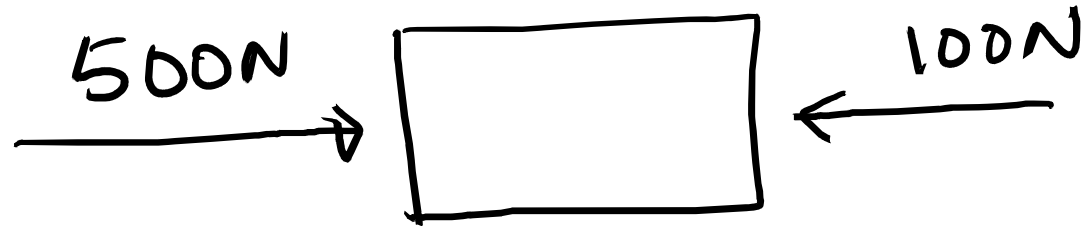
Net Pay:



Net pay

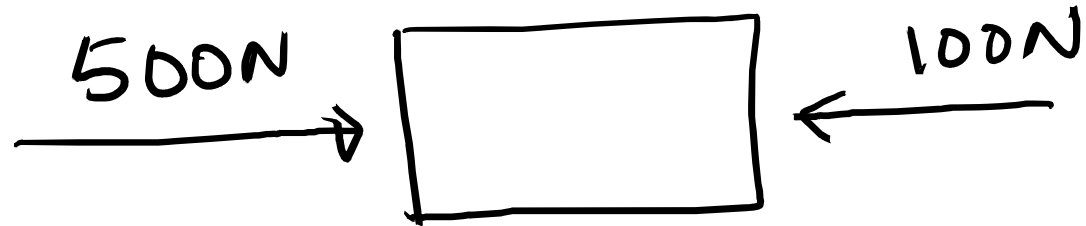


Net force



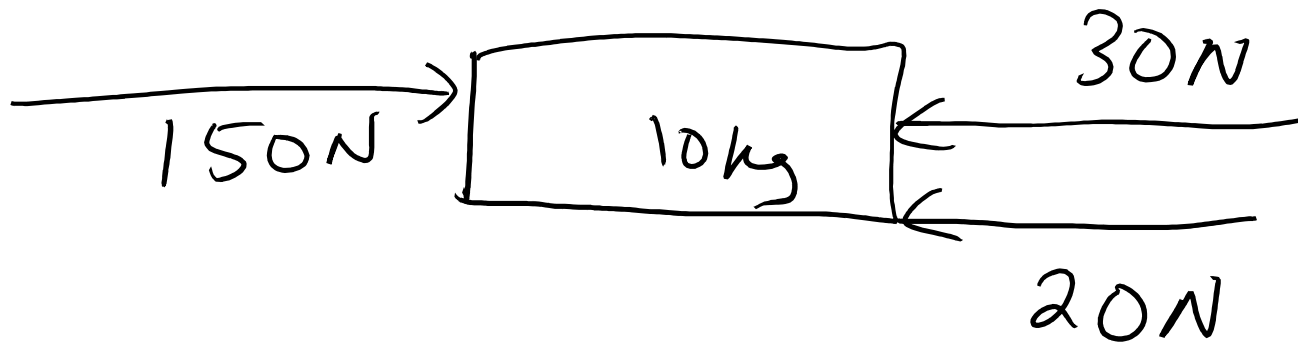
$$\begin{aligned} \text{Net force} = F_{\text{net}} &= \sum F = 500 + (-100) \\ &= 400\text{N} \end{aligned}$$

Net force

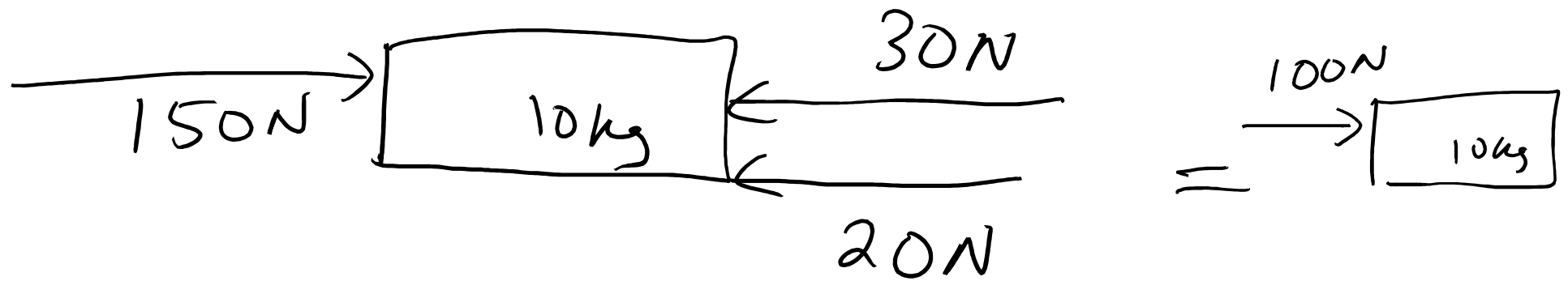


$$\begin{aligned} \text{Net force} = F_{\text{net}} &= \sum F = 500 + (-100) \\ &= +400\text{N} \end{aligned}$$





What is the acceleration?

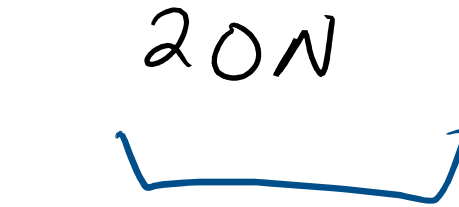
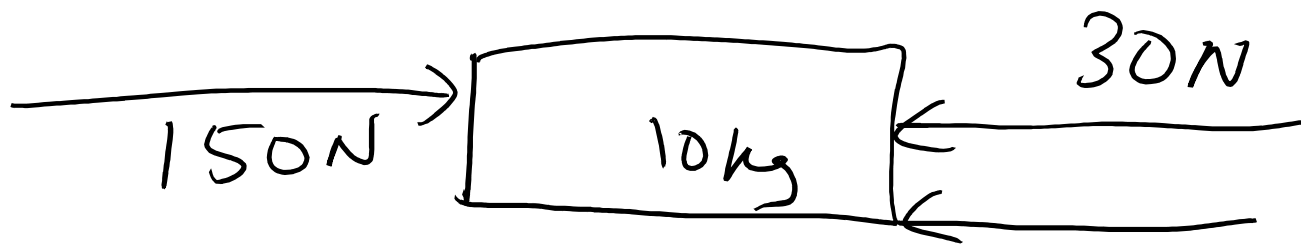


$$F_{\text{net}} = ma$$

$$150 + (-30) + (-20) = ma$$

$$100 = 10(a)$$

$$\underline{10 \text{ m/s}^2 = a}$$



This force
overpowers

$$\therefore 150 - (50) = 100 \text{ N}$$



EX

A 900 kg object is accelerated from rest to 12.0 m/s in 8.00 seconds along a straight road. How large is the force.

$$F_{\text{net}} = ma$$

$$a = \frac{v - u}{t}$$

$$F = 900 (1.5)$$

$$= 1350 \text{ N}$$

1350 N

$$= \frac{12 - 0}{8} = 1.5 \text{ m/s}^2$$