

EXAMINATIONS COUNCIL OF ZAMBIA

Joint Examination for the School Certificate  
and General Certificate of Education Ordinary Level

**ADDITIONAL MATHEMATICS 4030/2**  
**PAPER 2**

Tuesday

28 OCTOBER 2014

Additional materials:

Answer Booklet

Mathematical tables/Electronic calculators

Graph paper (1 sheet)

**TIME: 2 hours 30 minutes**

**INSTRUCTIONS TO CANDIDATES**

Write your name, centre number and candidate number in the spaces on the separate answer booklet provided.

There are **twelve (12)** questions in this paper. Answer **all** questions.

Write your answers on the Answer Booklet provided.

If you use more than one Answer Booklet, fasten the Answer Booklets together.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.

**INFORMATION FOR CANDIDATES**

The number of marks is shown in brackets [ ] at the end of each question or part question.

The total number of marks for this paper is 100.

**The use of a non programmable electronic calculator is expected, where appropriate.**

**Cell phones should not be brought in the examination room.**

Check the formulae overleaf

## Mathematical Formulae

### 1 ALGEBRA

*Quadratic Equation*

For the equation  $ax^2 + bx + c = 0$ ,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

### 2 SERIES

Arithmetic  $S_n = \frac{1}{2}n [2a + (n - 1)d]$

Geometric  $S_n = \frac{a(1-r^n)}{1-r}$  ( $r \neq 1$ )

$$S_{\infty} = \frac{a}{1-r} \text{ for } |r| < 1$$

### 3 TRIGONOMETRY

*Identities*

$$\sin^2 A + \cos^2 A = 1.$$

$$\sec^2 A = 1 + \tan^2 A.$$

$$\operatorname{cosec}^2 A = 1 + \cot^2 A.$$

Formula for  $\Delta ABC$

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A.$$

$$\Delta = \frac{1}{2} bc \sin A$$

### 4 STATISTICS

*Mean and standard deviation*

*Ungrouped data*

$$\text{Mean } (\bar{x}) = \frac{\sum x}{n}, \text{ SD} = \sqrt{\left\{ \frac{\sum (x - \bar{x})^2}{n} \right\}} = \sqrt{\left\{ \frac{\sum x^2}{n} - (\bar{x})^2 \right\}}$$

*Grouped data*

$$\text{Mean } (\bar{x}) = \frac{\sum fx}{\sum f}, \text{ SD} = \sqrt{\left\{ \frac{\sum f(x - \bar{x})^2}{\sum f} \right\}} = \sqrt{\left\{ \frac{\sum fx^2}{\sum f} - (\bar{x})^2 \right\}}$$

**1** Solve the simultaneous equations

$$p - 3q + 2r = 2,$$

$$2p - q + r = 5,$$

$$2p + q + 4r = -3.$$

[6]

**2 (a)** Find the range of values of  $x$  for which  $4x^2 - 8x - 5 \geq 0$ .

[3]

**(b)** Express  $7 - 5x - 2x^2$  in the form  $a(x + b)^2 + c$ , where  $a$ ,  $b$  and  $c$  are constants.

Hence, find the co-ordinates of the maximum turning point.

[4]

**3 (a)** Find the value of  $p$ , given that the expression  $2x^3 + px^2 - x - 2$  is divisible by  $x + 3$ .

[3]

**(b)** Factorise the expression  $2x^3 - 11x^2 + 17x - 6$ .

[4]

**4** Solve the equations

**(a)**  $3^{2x+1} - 3^x = 4,$

[4]

**(b)**  $\lg(3x + 2) + 6 \lg 2 = 2 + \lg(2x + 1).$

[3]

**5 (a)** A family consists of a father, mother and six children. Find the number of ways of arranging them in a straight line if

**(i)** there are no restrictions,

[2]

**(ii)** the arrangements start and end with a parent.

[2]

**(b)** A chess team consisting of 8 boys and 5 girls is to be chosen from 10 boys and 7 girls.

In how many ways can this be done?

[3]

**6** Find all the angles between  $0^\circ$  and  $360^\circ$  which satisfy the equations

**(a)**  $\sin 2x = -0.645,$

[3]

**(b)**  $5 \sin x - 3 \cos x = 0,$

[2]

**(c)**  $3 \tan^2 x + 5 = 7 \sec x.$

[4]

7 The table below shows a record of performance of pupils at school A and school B.

<b>School A</b>	1	1	2	3	3	3	4	6	6	6
<b>School B</b>	1	2	2	4	5	5	5	5	6	6

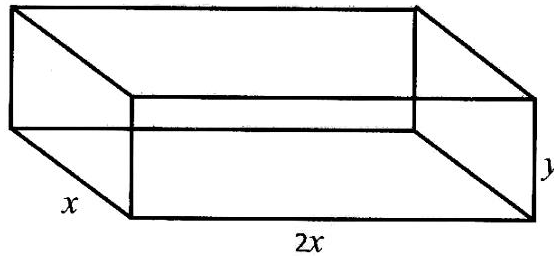
(a) Find the mean performance of each school. [2]

(b) Calculate the standard deviation for each school. [6]

(c) Which of the two schools has better results? Give a reason for your answer. [1]

8 (a) Find  $\int \left( x^3 + \frac{1}{x^3} \right) dx$ . [2]

(b) The diagram below shows a rectangular box made up of a thin sheet of metal with a lid. The length of the box is  $2x$  cm, the breadth is  $x$  cm and the height is  $y$  cm.



(i) Given that the volume of the box is  $72\text{cm}^3$ , show that the surface area,  $A\text{cm}^2$ , of the thin sheet of metal used is given by  $A = 4x^2 + \frac{216}{x}$ . [3]

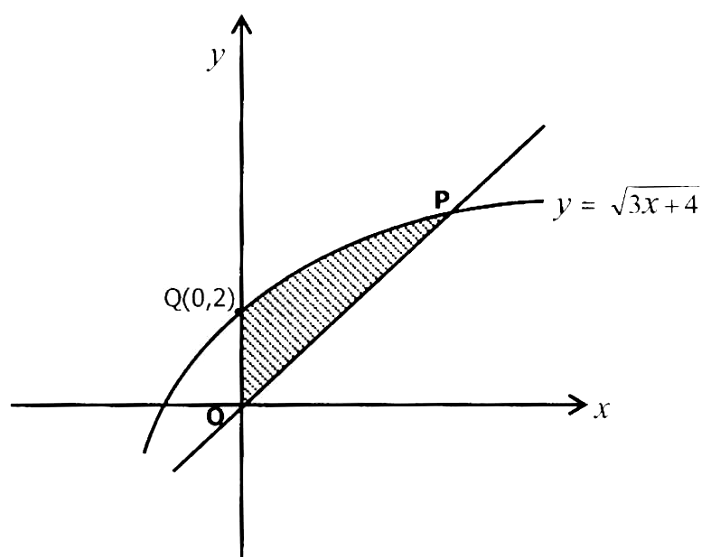
(ii) Given that  $x$  can vary, find the minimum area of the box. Show that this is a minimum value. [4]

9 (a) The eighth term of a geometric progression is 32 and the fourth term is 2. Find the first term and the positive value of the common ratio. [3]

(b) Find the sum to infinity of a geometric progression whose first term is 5 and the second term is  $-4$ . [2]

(c) The  $n$ th term of an arithmetic progression is  $3n + 7$ . Find the sum of the first 40 terms. [4]

- 10** The velocity in m/s of a particle, travelling in a straight line at time  $t$  seconds after leaving a fixed point O, is given by  $V = 10 + kt - 3t^2$ , where  $t \geq 0$  and  $k$  is a constant. When  $t = 0$  the particle is at O and its acceleration is  $1\text{m/s}^2$ . Find the
- (a) value of  $k$ , [3]
- (b) value of  $t$  when the particle is instantaneously at rest, [3]
- (c) distance the particle has travelled when it is again at O. [4]
- 11** The diagram shows part of the curve  $y = \sqrt{3x+4}$  and a straight line. The curve meets the straight line at P. The gradient of the straight line is 1.



- (a) Find
- (i) the equation of the straight line OP, [1]
- (ii) the co-ordinates of the point P. [3]
- (b) The shaded region is rotated through  $360^\circ$  about the  $x$ -axis to form a solid of revolution. Calculate the volume generated in terms of  $\pi$ . [6]

**12 Answer only one of the following alternatives:**

**EITHER**

- (a) A tangent touches the curve  $y = 3x^2 + 2x + 1$  at the point where it is parallel to the line  $4x + y = 5$ . Find the co-ordinates of the point where the tangent touches the curve. [3]
- (b) (i) Draw the graph of  $y = e^{2x} - 4$  for values of  $x$  at intervals of 0.5, for  $-2 \leq x \leq 1\frac{1}{2}$ . [4]
- (ii) By drawing a suitable straight line on your graph, obtain an approximate solution to the equation  $x = \ln \sqrt{1-4x}$ . [3]

**OR**

- (a) The sixth term of an arithmetic progression with 12 terms is 14 and the sum of the last six terms is 126. Calculate the sum of the first six terms. [5]
- (b) The fifth term of a geometric progression is  $\frac{2}{81}$  and the sum of the third and fourth terms is  $\frac{8}{27}$ . Find the
- (i) positive value of the common ratio,  $r$ , [3]
- (ii) sum to infinity of the progression. [2]