

AEN 4131 – FARM STRUCTURES

ASSIGNMENT 3

Due date: Thursday: 26/05/2022

Question

The beam shown in Fig. Q, has a pin support at A and a (roller) smooth support at B.

- i) Determine the reaction forces at the supports A and B.
- ii) Draw the shear force diagram (SFD) and bending moment diagram (BMD) for the beam.
- iii) Give the value of the maximum shear force and state its location.
- iv) Give the value of the maximum bending moment and state its location.

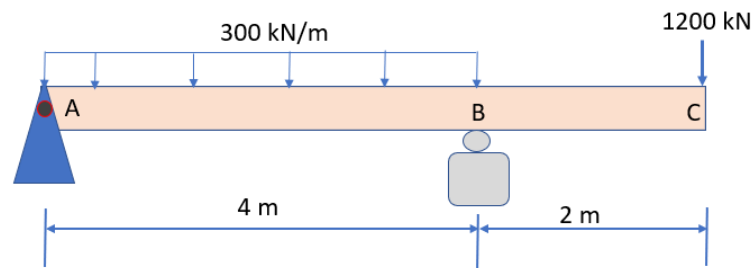


Fig. Q

NOTE: Since the loading changes at one point (point B), there are two sections to be analysed. Check the example below for a better understanding.

EXAMPLE

On a particular day, one beam supported 20kN/m of the weight of the first floor of a storage building which included the maize stored on the floor. On that day, the farmer who owns the structure was using the beam to hoist a 450kN load into a right truck. The hoist was placed in the middle of the beam span as shown in Fig.QE.

- i. Determine the reactions at A and C
- ii. Draw the shear force and bending moment diagrams for the beam
- iii. State the maximum absolute values of the shear force and bending moment and indicate the location with respect to point A.

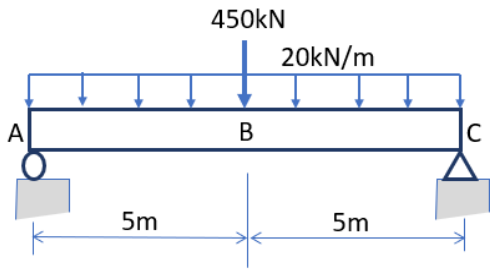


Fig. QE

Solution

- i. **Determine the reactions at A and C**

$$R_A + R_C - 450 - 20 \cdot 10 = 0$$

$$R_A + R_C = 650 \text{ kN} \dots\dots\dots(1)$$

Summation of moments about A = 0. Clockwise positive

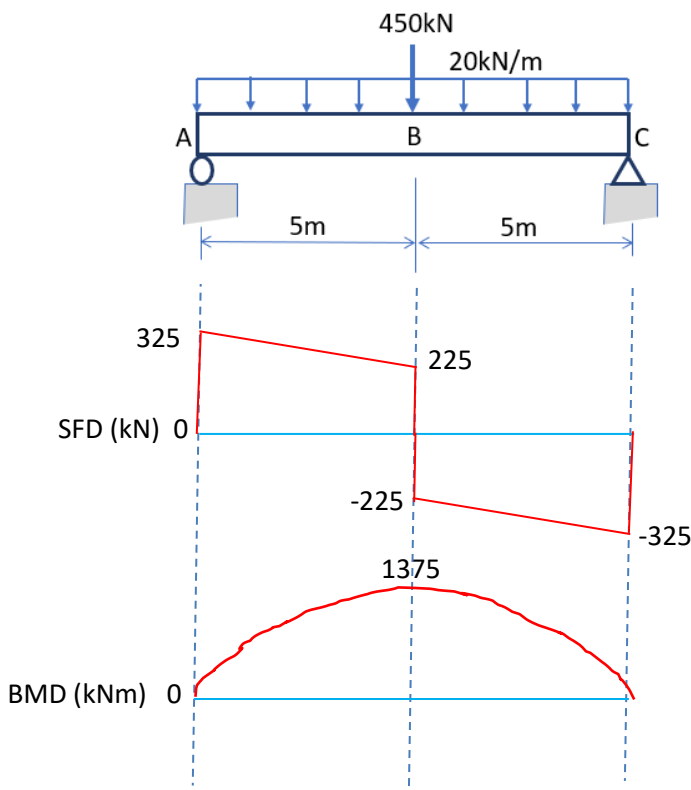
$$450 \cdot 5 + 200 \cdot 5 - 10R_C = 0$$

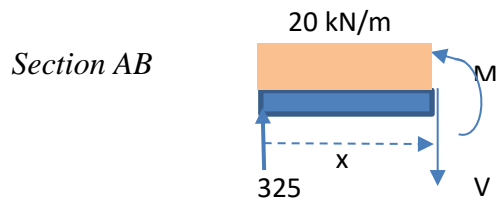
$$R_C = 325 \text{ kN}$$

$$R_A = 650 - 325 = 325 \text{ kN}$$

- ii. **Draw the shear force and bending moment diagrams for the beam**

Since the loading of the beam is changed at one point (point B), two sections of the beam are analysed.





$$325 - 20x - V = 0$$

$$V = 325 - 20x$$

For $x = 0$, $V = 325$ kN

For $x = 5$, $V = 325 - 100 = 225$ kN

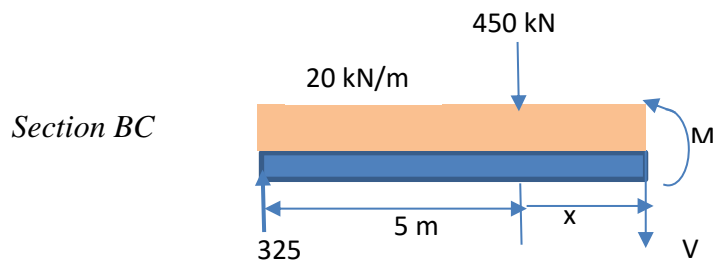
Moments about x, clockwise positive

$$325x - 10x^2 - M = 0$$

$$M = 325x - 10x^2$$

For $x = 0$, $M = 0$

For $x = 5$, $M = 325 \cdot 5 - 10 \cdot 25 = 1375$ kNm



$$325 - 20(5+x) - 450 - V = 0$$

$$V = 325 - 100 - 450 - 20x$$

$$V = -225 - 20x$$

For $x = 0$, $V = -225$ kN

For $x = 5$, $V = -325$ kN

Moments about x, clockwise positive

$$325(5+x) - (20 \cdot 5)(2.5+x) - 10x^2 - 450x - M = 0$$

$$M = 1625 + 325x - 250 - 100x - 10x^2 - 450x$$

$$= 1375 - 225x - 10x^2$$

For $x = 0$, $M = 1375$ kNm

For $x = 5$, $M = 0$

- iii. **State the maximum absolute values of the shear force and bending moment and indicate the location with respect to point A.**

Maximum shear force = 325 kN at A and C

Maximum bending moment = 1375 kNm at B